

Using the Reactance Chart for Filter Design Problems

H. B. DAVIS*

Calculations of components for various filter and equalizer circuits are simplified by graphical means.

THE VALUE OF the reactance chart such as that shown in Fig. 1 is becoming more and more widely recognized as time goes on. Although it was originally indicated by Slosszewsky that the chart could be used for other purposes than reactance and resonant-frequency calculations, it is still largely used for that purpose. The other short-cuts offered by the chart have been largely neglected.

It has been known for some time that these charts could be used for certain filter calculations. It is the purpose of this article to show why this is true and how it may be done for several popular types of filters. Although the material may not be new to many readers, it is felt that there are others to whom the information may be of value.

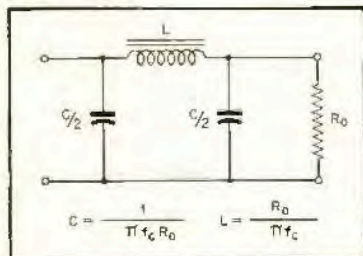


Fig. 2. Low-pass filter prototype, or constant- k section. R_0 is the terminating resistance; f_c is cut-off frequency.

The chart is designed to solve equations of three parameters in which 2π enters as a factor. Specifically it solves such equations as

$$X_L = 2\pi fL \quad (1)$$

$$X_C = \frac{1}{2\pi fC} \quad (2)$$

$$f = \frac{1}{2\pi\sqrt{LC}} \quad (3)$$

Solving for L and C in equations (1) and (2) gives

$$L = \frac{X_L}{2\pi f} \quad (4)$$

*7721 Old Georgetown Rd., Bethesda 14, Md.

$$C = \frac{1}{2\pi fX_C} \quad (5)$$

The chart may be used to solve these or other three-parameter equations having 2π as a factor if the equation to be solved can be put into one of these or an equivalent form.

Inductive and capacitive reactance have the dimensions of resistance. Therefore, without changing the form of the equations of the ordinate of the chart equations, (1) and (2) may be written

$$R_L = 2\pi fL \quad (6)$$

$$R_C = \frac{1}{2\pi fC} \quad (7)$$

Solving equations (6) and (7) for L and C respectively gives

$$L = \frac{R_L}{2\pi f} = \frac{1}{2} \cdot \frac{R_L}{\pi f} \quad (8)$$

$$C = \frac{1}{2\pi fR_C} = \frac{1}{2} \cdot \frac{1}{\pi fR_C} \quad (9)$$

Equations (8) and (9) are seen to be very similar to the equations for the low-pass filter prototype shown in Fig. 2. The equations indicate, however, that the values given by the reactance chart for L and C will be equal to one half of the value calculated from the prototype equations if R_0 is substituted for R_L and R_C and f_c is substituted for f .

For example, if it is desired to design a 10,000-ohm filter section with a cut-off frequency f_c of 1,000 cps, substituting these values in the equations of Fig. 2 give

$$L = \frac{10,000}{\pi \times 1000} = 3.18H, \text{ and}$$

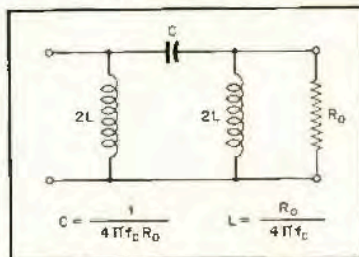


Fig. 3. High-pass filter prototype, or constant- k section.

$$C = \frac{1}{\pi \times 1000 \times 10,000} = 0.0318 \mu f$$

Using the reactance chart and entering the chart at $R_0=10,000\Omega$ at the intersection with the 1000 cps vertical, it

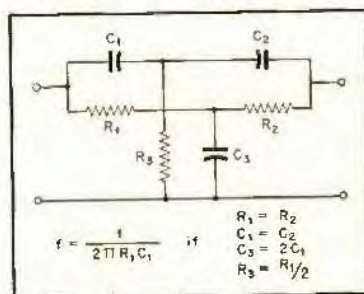
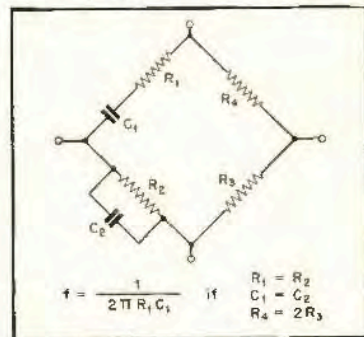


Fig. 4 (above). Parallel-T rejection or null network configuration.

Fig. 5. (below). Wien bridge circuit as employed in RC oscillators.



is found that L is given as 1.59 Henrys and C is 0.0159 μf . These values are exactly half of the values found from the equations.

In a similar manner, if f_c is substituted for f and R_0 for X_L and X_C in equations (4) and (5), equations (10) and (11) result.

$$L = \frac{R_0}{2\pi f_c} \quad (10)$$

$$C = \frac{1}{2\pi f_c R_0} \quad (11)$$

These equations are seen to be simi-

lar to the high-pass prototype equations shown in Fig. 3. Dividing both sides of equations (10) and (11) by two yields

$$\frac{L}{2} = \frac{R_o}{4\pi f_c}$$

$$\frac{C}{2} = \frac{1}{4\pi f_c R_o}$$

Solving these equations for L and C gives

$$L = 2 \times \frac{R_o}{4\pi f_c}$$

$$C = 2 \times \frac{1}{4\pi f_c R_o}$$

From these equations it is seen that the values of L and C obtained from

the reactance chart will be exactly twice the value obtained from the high-pass filter prototype equations. That this is true may be verified by solving the equations for the filters and comparing the results with the values obtained from the chart.

If equation (2) is solved for f and
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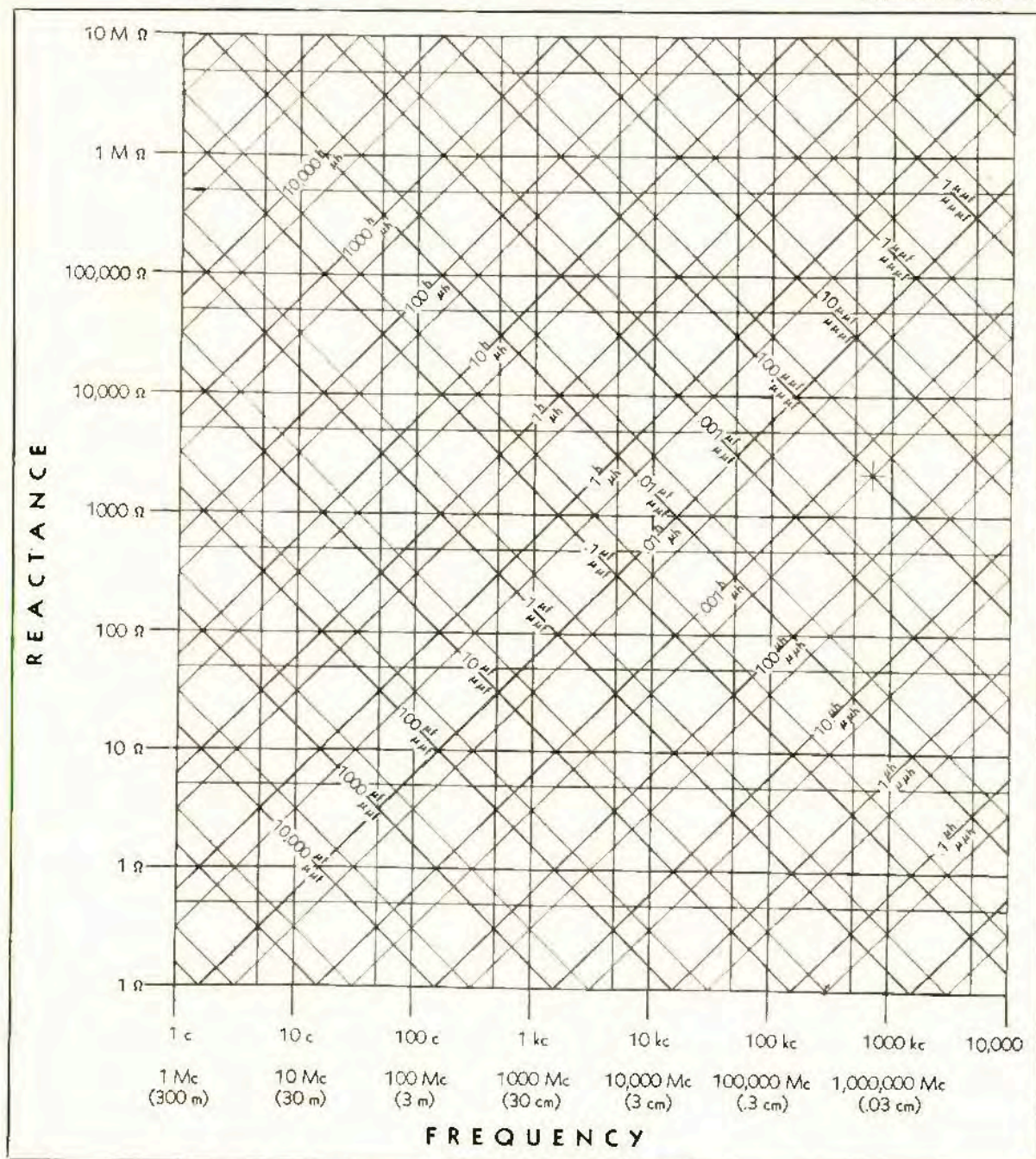


Fig. 1. The reactance chart, well known for its many applications in circuit calculations.

(Courtesy General Radio Company)

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R substituted for X , the equation becomes

$$f = \frac{1}{2\pi RC}$$

This equation will be recognized as the equation for the rejection frequency of the parallel-T filter, such as is shown in *Fig. 4* providing $C_1 = C_2$ and $R_1 = R_2$ with R_3 and C_3 properly proportioned. This filter is electrically equivalent to the Wein bridge shown in *Fig. 5*; consequently, the chart may also be used to determine the null frequency of such a bridge, or the frequency of an oscillator employing the Wein bridge for the frequency-determining element.

Thus, it has been shown that the conventional reactance chart may be used without modification for determining component values for the low-pass filter prototype if the values of L and C read from the chart are taken for $L/2$ and $C/2$. In the case of the high-pass filter the values indicated by the chart are twice the values given by the filter equations. The value of the series elements of a parallel-T rejection filter or Wein bridge, such as is used frequently in oscillators, are indicated directly on the chart.

Although graphical methods are not recommended for highly accurate work, the results obtained by using the chart are sufficiently accurate for many engineering applications.

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